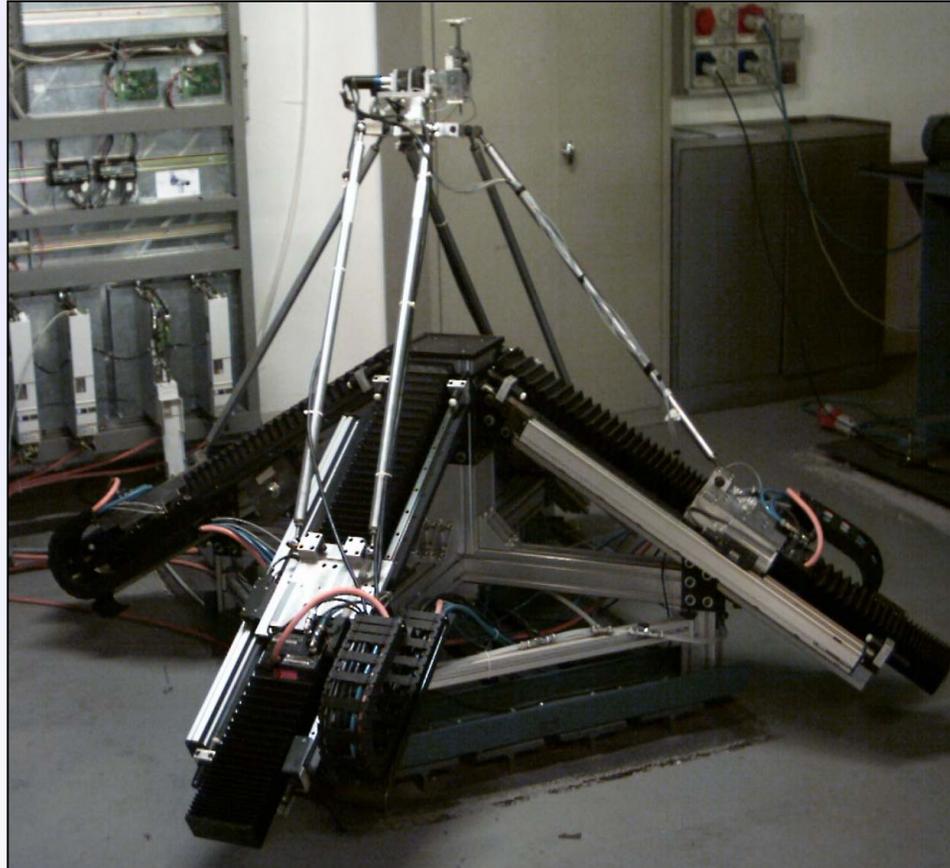


**Università degli Studi di Brescia Facoltà di Ingegneria**  
**Corso di Dottorato in Meccanica Applicata XVII Ciclo**



**Presentazione finale di**  
**Diego Tosi**

# **Progetto e Realizzazione di un Robot a Cinematica Parallela per Applicazioni Mediche**



# Specifiche di progetto

## Robot medici

✓ analisi dello stato dell'arte\*

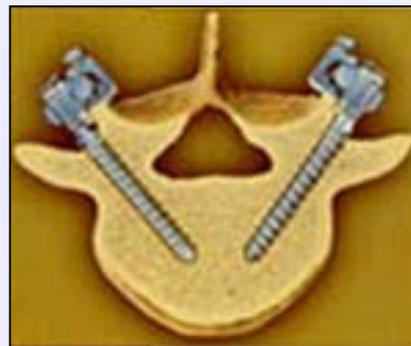


- ✓ spazio di lavoro: 400x400x300 mm
- ✓ inclinazione punta:  $\pm 40^\circ$
- ✓ velocità
- ✓ accelerazione

## Progetti

“**METAFORE**” e “**RIME**”

✓ prototipo di robot per il fissaggio di viti peduncolari

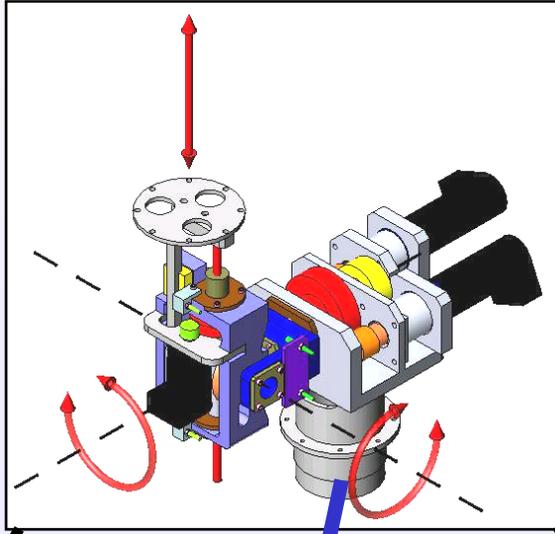


# Struttura cinematica ibrida



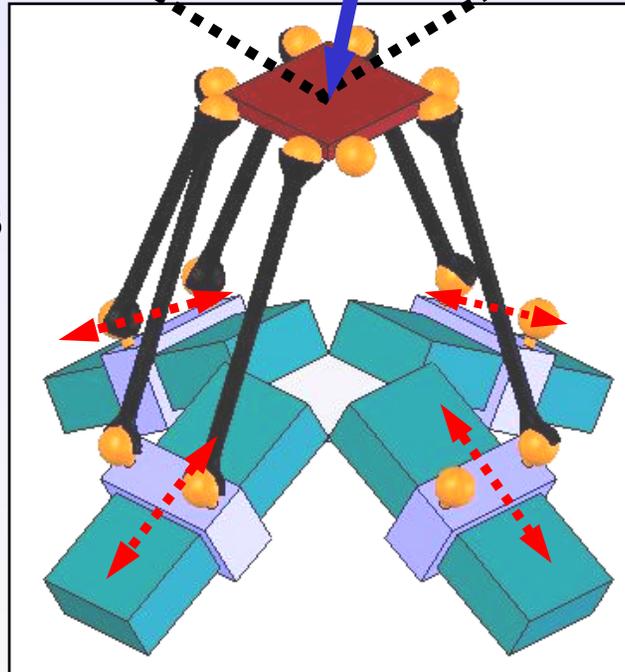
## parte seriale

- ✓ 3 gradi di libertà
- ✓ 2 rot. + 1 trasl.

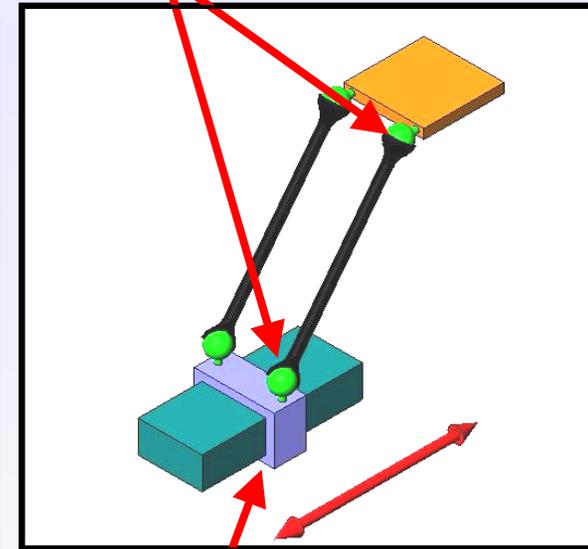


## parte parallela

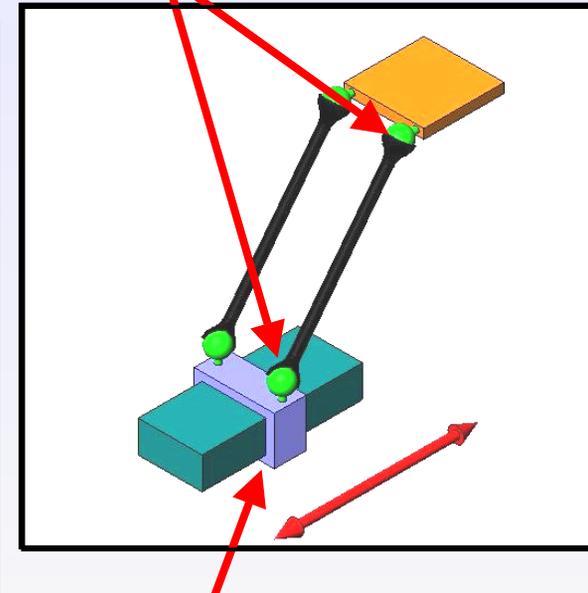
- ✓ base moveable points
- ✓ modulare
- ✓ 4 assi lineari
- ✓ riconfigurabile
- ✓ 3 o 4 gradi di libertà
- ✓ ridondante



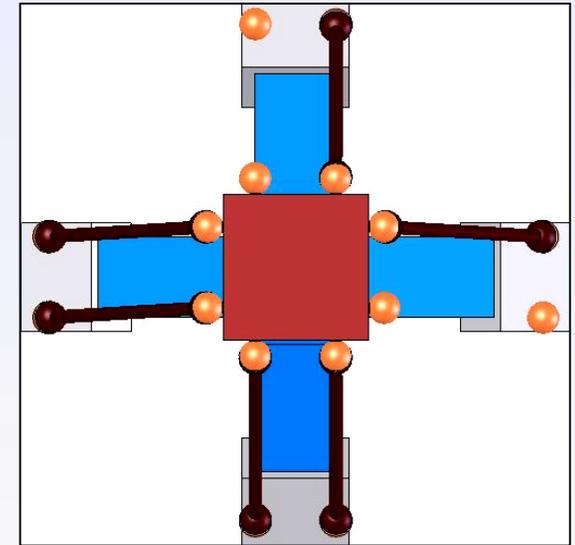
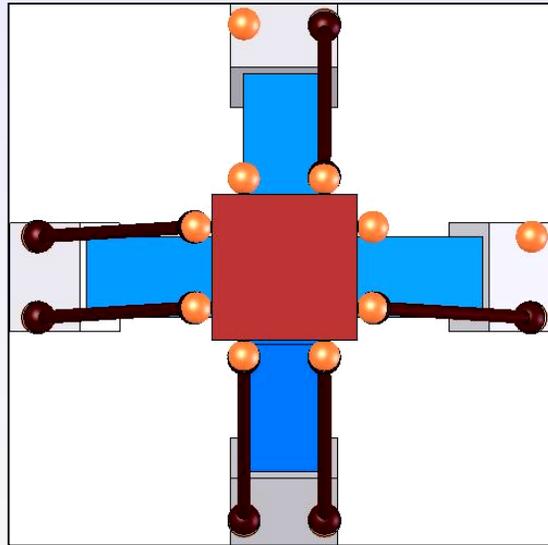
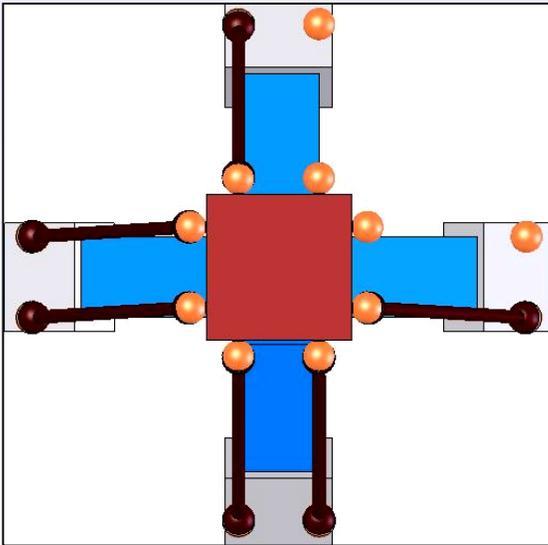
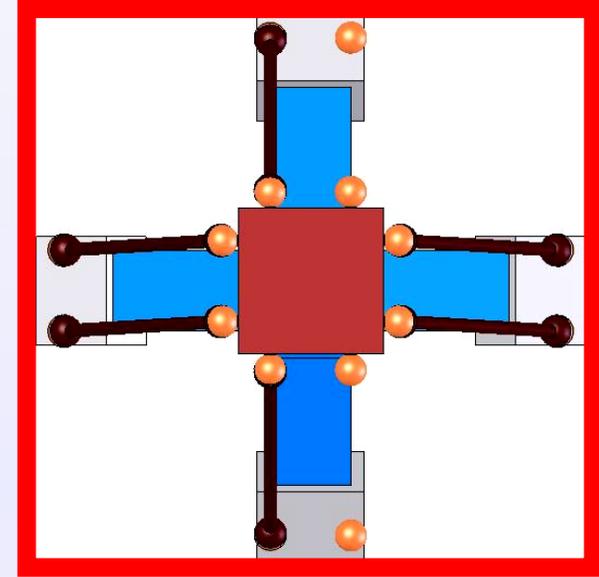
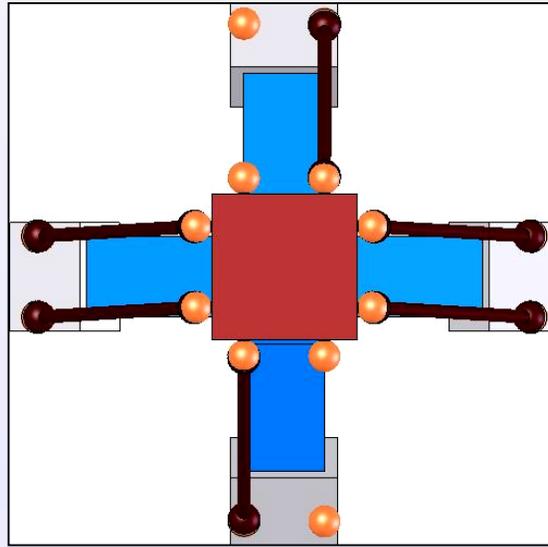
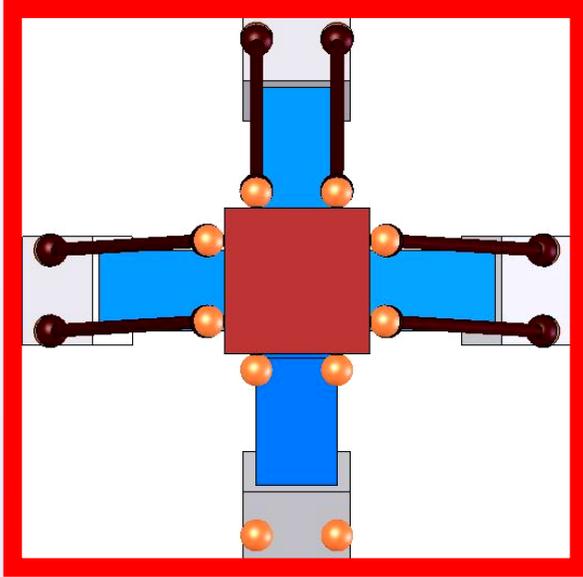
giunti sferici



giunto prismatico



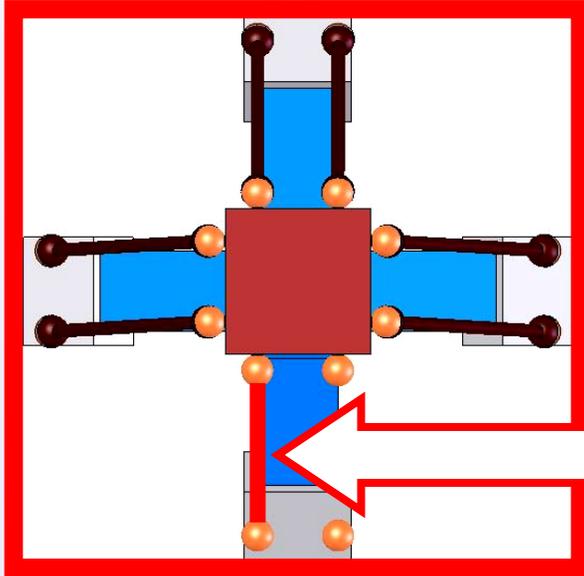
# Riconfigurabilità



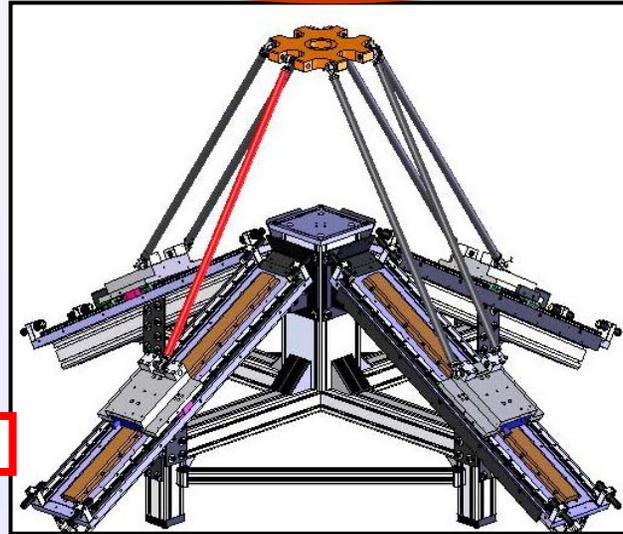
# Riconfigurabilità



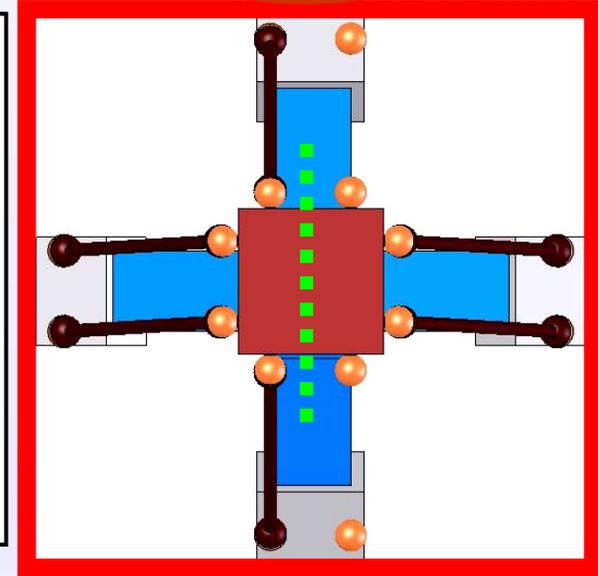
3 g.d.l.



3 g.d.l. rid.



4 g.d.l.



- ✓ 6 bielle su 3 motori
- ✓ 3 gdl
- ✓ solo traslazioni

- ✓ 7 bielle su 4 motori
- ✓ 3 gdl iperstatica
- ✓ 4° motore controllato in forza
- ✓ recupero dei giochi

- ✓ 6 bielle su 4 motori
- ✓ 4 gdl
- ✓ 3 traslaz.+1 rotaz.
- ✓ **asse rotaz. fisso**

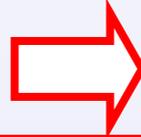
# Analisi struttura parallela

## STUDIO CINEMATICO: POSIZIONI



### Inversa

posizione piattaforma



posizioni motori

3 gdl e 4 gdl: risolta in forma chiusa

✓ Chiusura vettoriale

$$\begin{aligned} \mathbf{O}_j + q_j \mathbf{n}_j + l \mathbf{w}_j &= \mathbf{X}_p + \mathbf{a}_j & \mathbf{r}_j &= \mathbf{X}_p + \mathbf{a}_j - \mathbf{O}_j, \\ q_j &= \mathbf{n}_j^T \mathbf{r}_j \pm \sqrt{(\mathbf{n}_j^T \mathbf{r}_j)^2 - (|\mathbf{r}_j|^2 - l_j^2)} \end{aligned}$$

### Diretta

posizioni motori



posizione piattaforma

3 gdl: risolta in forma chiusa

✓ Geometria solida  
✓ Algebra matriciale

4 gdl: risolta numericamente

✓ Equazione trascendente (8° grado)  
✓ Soluzione approssimata  
✓ Newton-Raphson su 2 equazioni

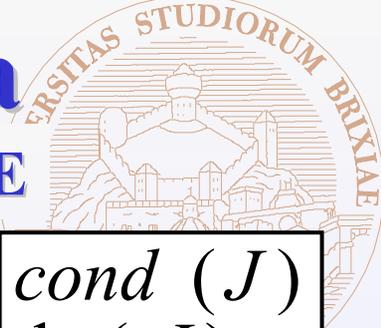
$$\begin{cases} (\mathbf{Q}'\mathbf{H})^T \mathbf{X}_p + \mathbf{k}_A = 0; \\ (\mathbf{Q}'\mathbf{H})^T \mathbf{X}_p + \mathbf{k}_B = 0; \end{cases} \quad \mathbf{X}_p = \mathbf{X}_A + \lambda (\mathbf{X}_B - \mathbf{X}_A) / |\mathbf{X}_B - \mathbf{X}_A|$$

$$(\lambda)^2 + 2\lambda (\mathbf{X}_A - \mathbf{Q}'_1)^T (\mathbf{X}_B - \mathbf{X}_A) / |\mathbf{X}_B - \mathbf{X}_A| + (|\mathbf{X}_A|^2 - 2\mathbf{Q}'_1 \mathbf{X}_A + \text{cost}_1)$$

$$\begin{aligned} Eq_a(\alpha, z) &= (x(z, \alpha) - \text{cost}_a + a \cos(\alpha) - q_1 \cos(\psi))^2 + y(z, \alpha)^2 + \\ &\quad + (z - \text{cost}_z - a \sin(\alpha) + q_1 \sin(\psi))^2 - l^2 \\ Eq_b(\alpha, z) &= (x(z, \alpha) + b - b \cos(\alpha))^2 + (y(z, \alpha) - \text{cost}_a + a - q_2 \cos(\psi))^2 + \\ &\quad + (z - \text{cost}_z + b \sin(\alpha) + q_2 \sin(\psi))^2 - l^2 \end{aligned}$$

# Analisi struttura parallela

## MAPPATURA INDICI DI PRESTAZIONE



$$dQ = JdS$$

$dQ$  spostamento motori

$J$  matrice jacobiana

- $cond(J)$
- $\det(J)$
- $\sigma_{\min}(J)$
- $\sigma_{\max}(J)$

$$dS = KF_s$$

$dS$  spostamento e rotaz. piattaforma

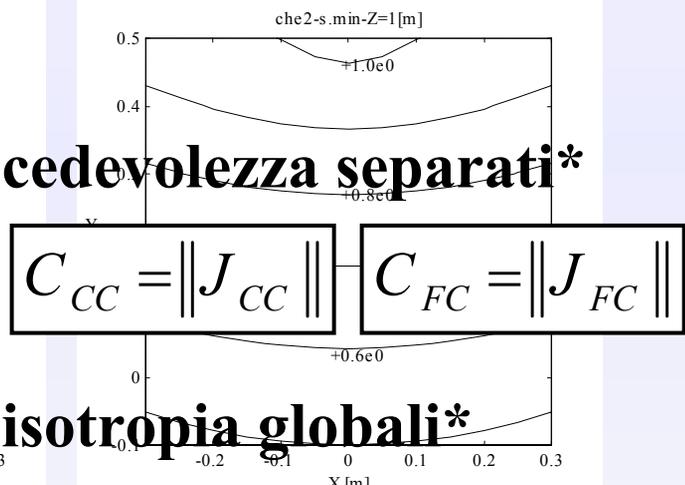
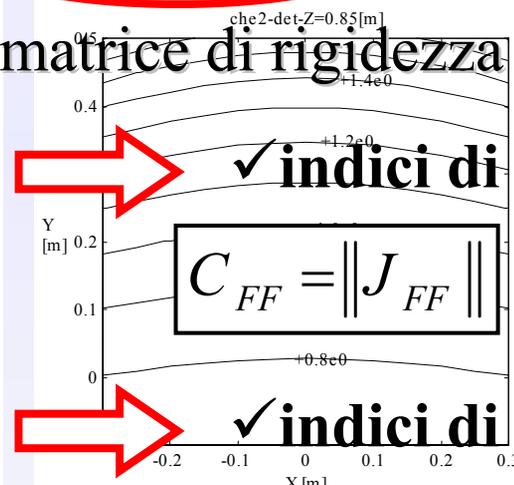
$F_s$  forze e coppie sulla piattaforma

$$K = \begin{bmatrix} J_{FF} & J_{FC} \\ J_{CF} & J_{CC} \end{bmatrix}$$

$K$  matrice di rigidezza

**✓ indici di cedevolezza separati\***

**✓ indici di isotropia globali\***



$$c_f = \frac{\sigma_{\max}(J_{FF})|F_{\max}| + \sigma_{\max}(J_{FC})|C_{\max}|}{\sigma_{\min}(J_{FF})|F_{\max}| + \sigma_{\min}(J_{FC})|C_{\max}|}$$

$$c_c = \frac{\sigma_{\max}(J_{CC})|C_{\max}| + \sigma_{\max}(J_{CF})|F_{\max}|}{\sigma_{\min}(J_{CC})|C_{\max}| + \sigma_{\min}(J_{CF})|F_{\max}|}$$

# Analisi struttura parallela



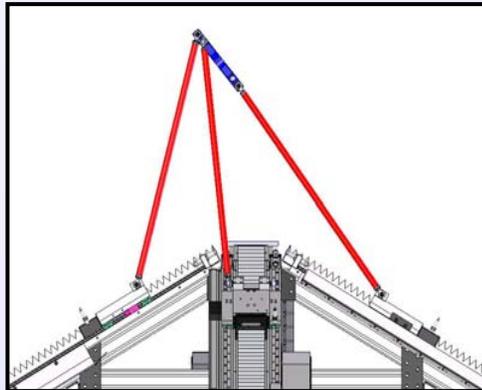
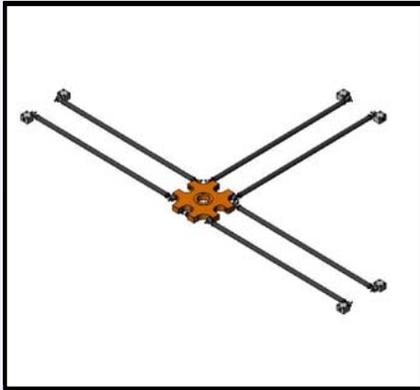
## CONFIGURAZIONI SINGOLARI

## STUDIO DINAMICO

3 & 4 gdl

4 gdl

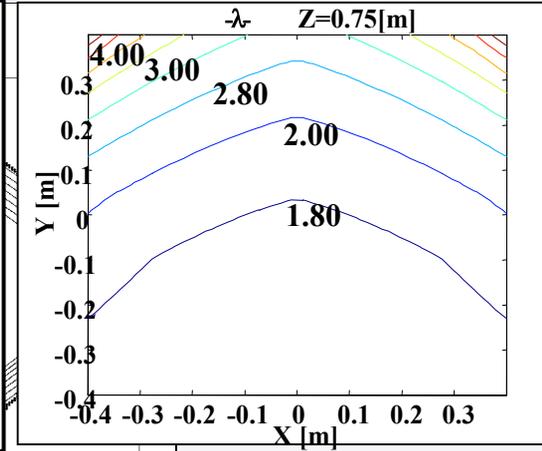
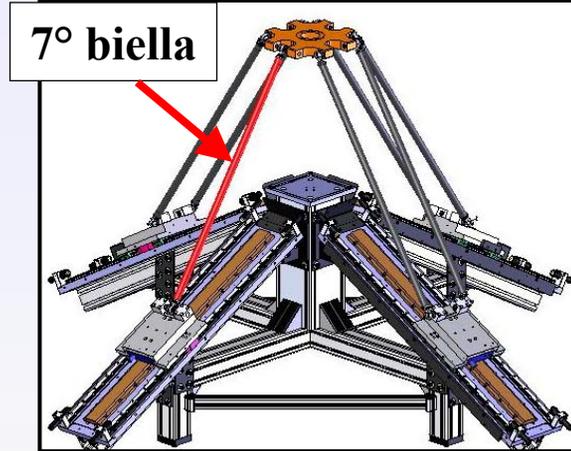
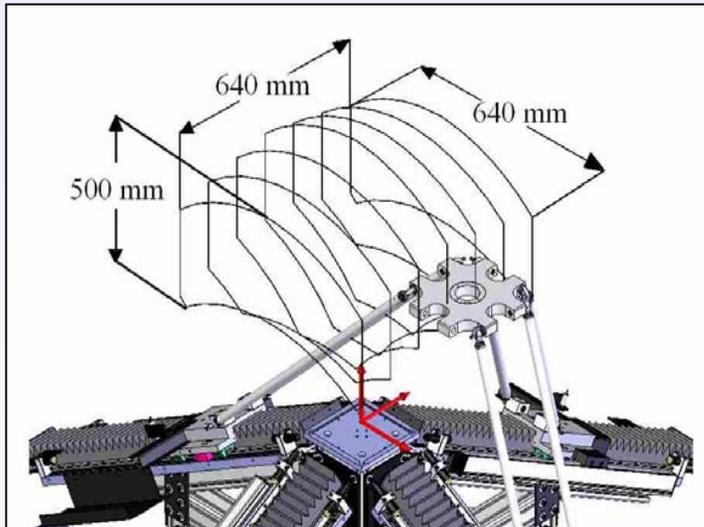
- ✓ 3 e 4 gdl
- ✓ corpi rigidi
- ✓ massa delle bielle
- ✓ scelta degli attuatori lineari
- ✓ modello dell'attrito



$$\mathbf{F}_m - (\mathbf{M}_m + \mathbf{J}^T \mathbf{M}_p \mathbf{J}) \ddot{\mathbf{q}} + \mathbf{J}^T \mathbf{M}_p \dot{\mathbf{J}} \dot{\mathbf{q}} + (\mathbf{P}_n + \mathbf{J}^T \mathbf{F}_e) = 0$$

## SPAZIO DI LAVORO

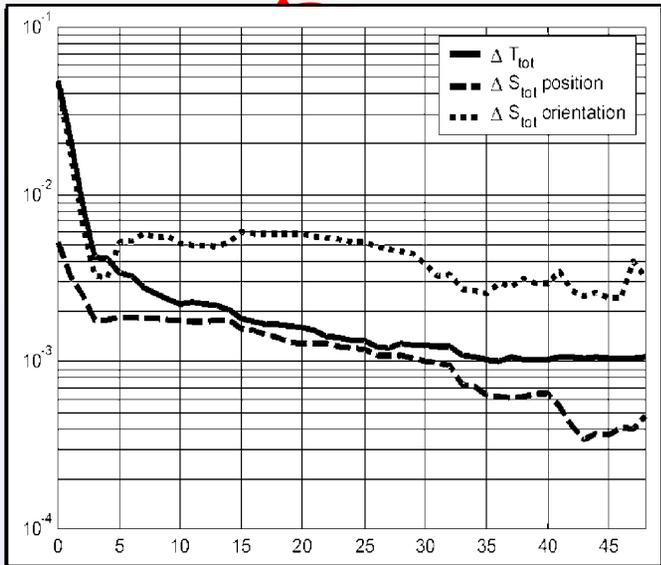
## RECUPERO DEI GIOCHI



$$\mathbf{F}_{rid} \approx 2 \div 3 \mathbf{F}_{esterna applicata}$$

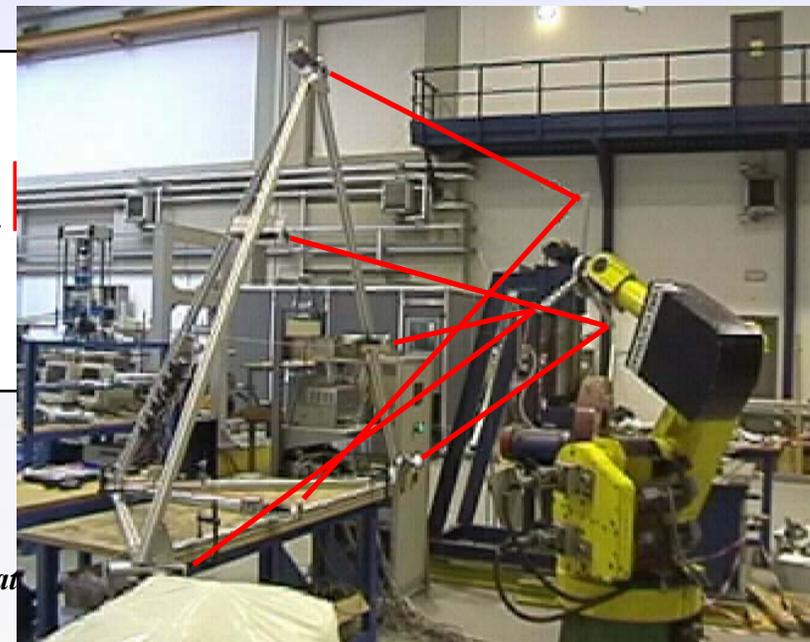
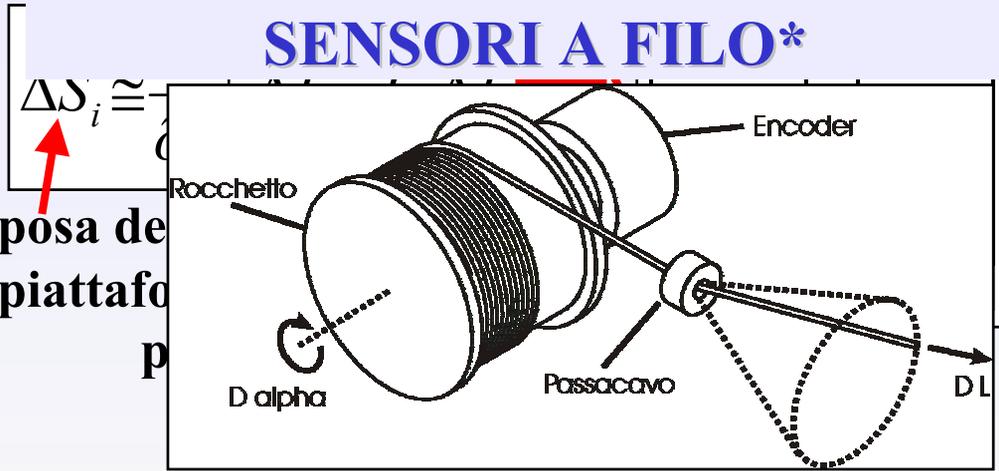


# Calibrazione struttura parallela



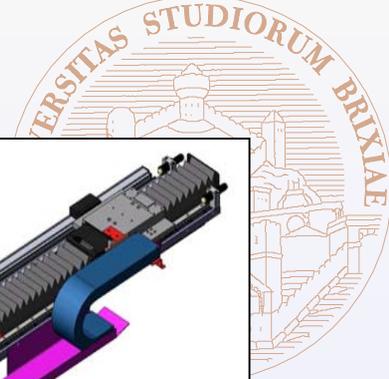
- ✓ modello parametrico M.C.P.C. 48 parametri di cui 36 interni
- ✓ sensori interni ed esterni inclinometri, ecoder sui giunti cardanici, 4° asse trascinato
- ✓ simulazione di calibrazione

## ELIMINAZIONE DEI PARAMETRI TRAMITE SVD\* CALIBRAZIONE CON SENSORI A FILO\*

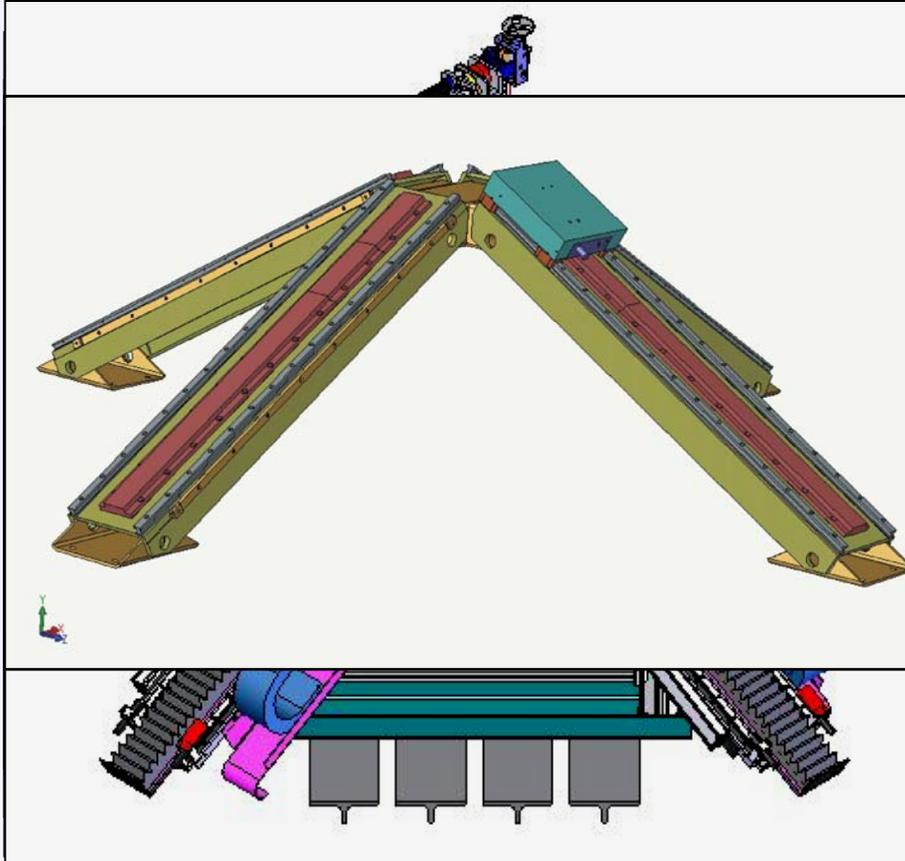


\*De Foa, G. Legnani, *Calibration of a Parallel Serial Hybrid Redundant Manipulator*, Proc. of ISRA 2003, Chicago, Illinois, 2003.  
\*De Foa, G. Legnani, *Calibration procedure for industrial robots*, Proc. of ISR 2004, Paris 23-26/3/04

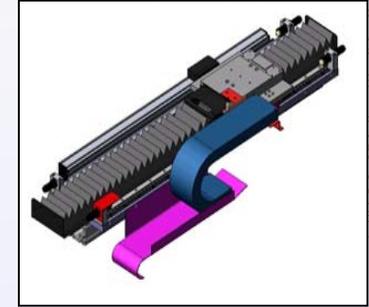
# Progettazione



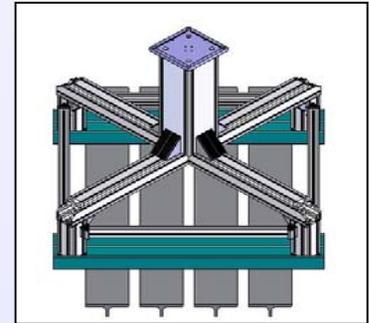
## Progetto finale



✓ Assi lineari



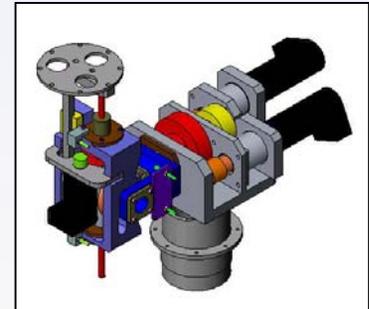
✓ Telaio



✓ Piattaforma

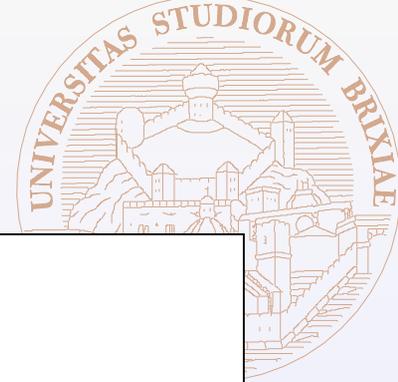


✓ Polso seriale



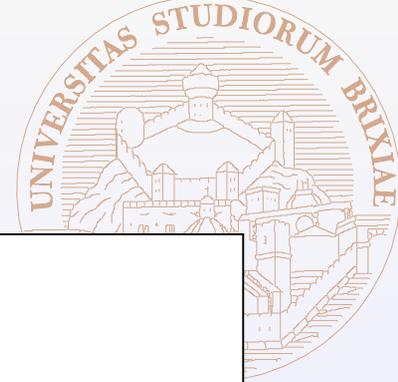
# Progettazione

## ASSE LINEARE

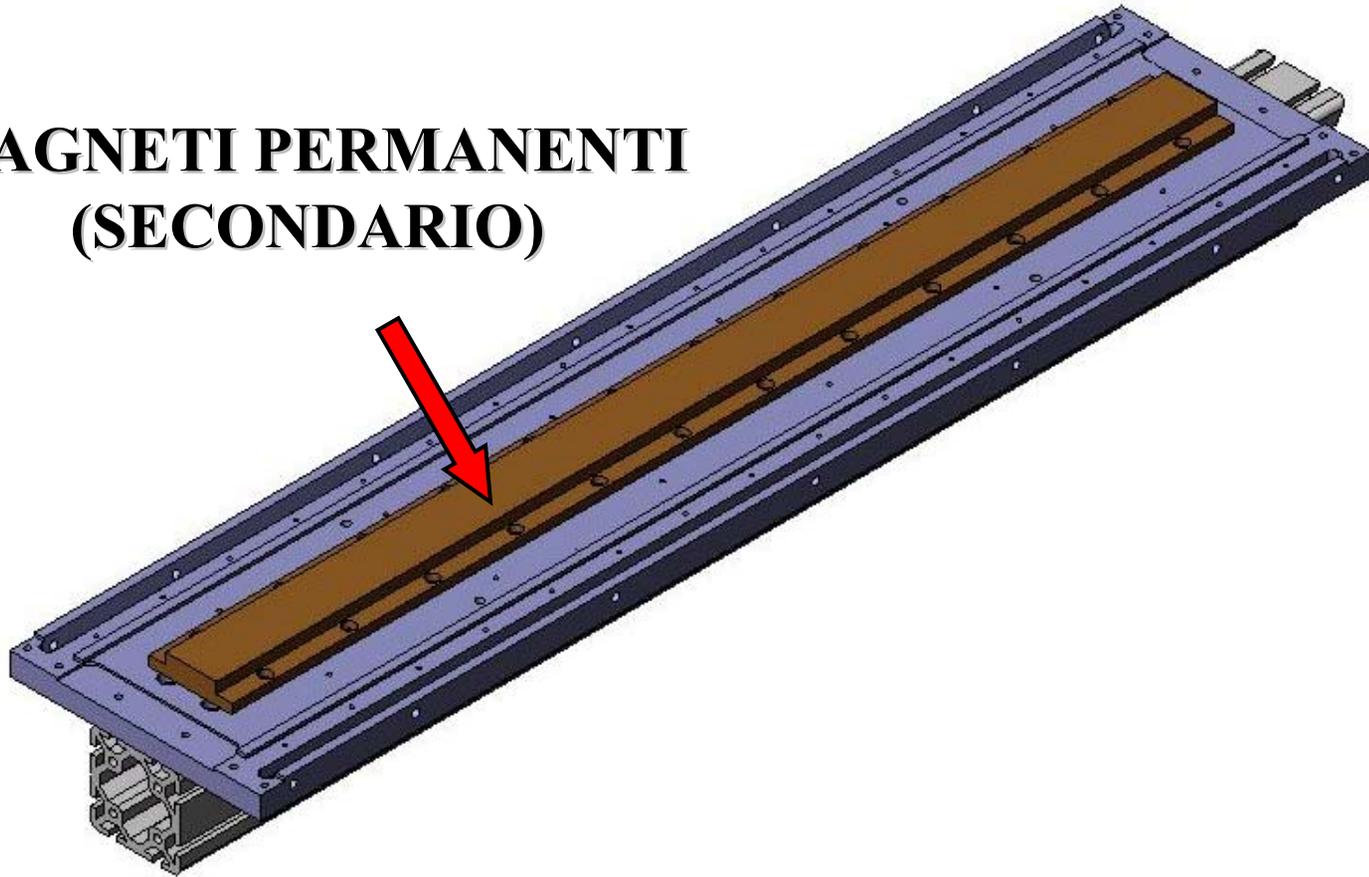


# Progettazione

## ASSE LINEARE

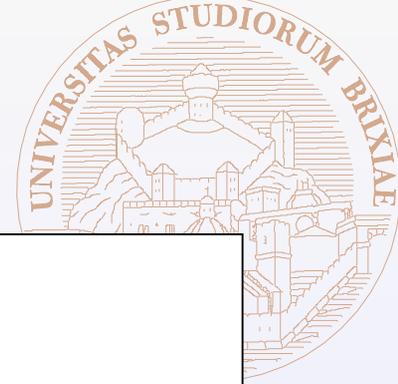


**MAGNETI PERMANENTI  
(SECONDARIO)**

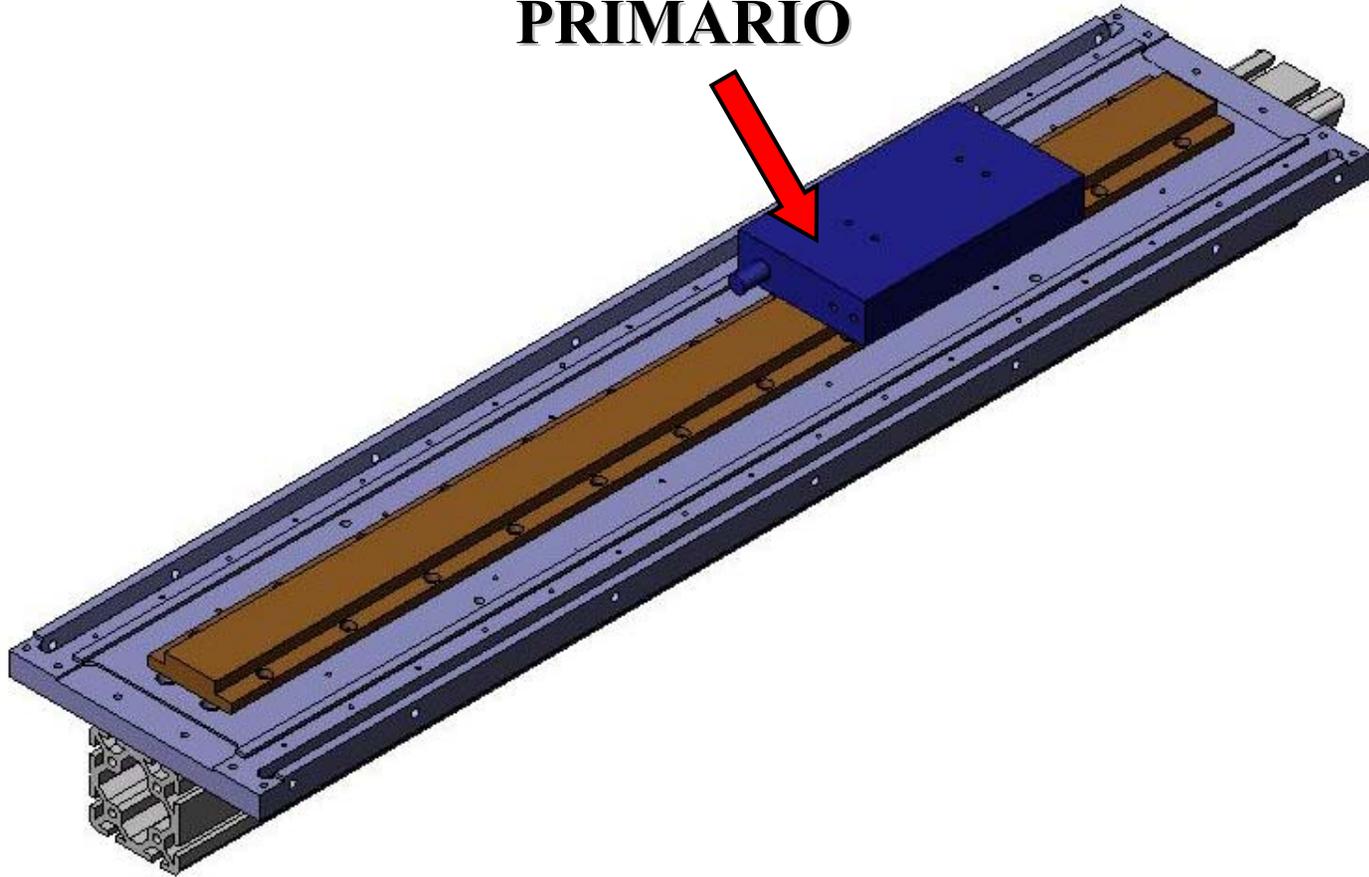


# Progettazione

## ASSE LINEARE

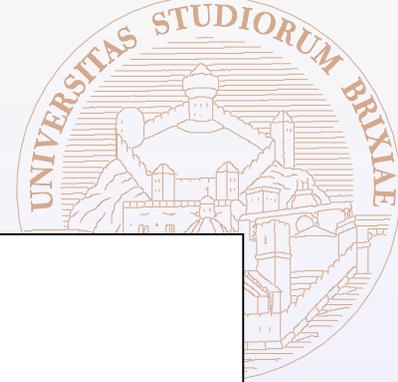


**PRIMARIO**

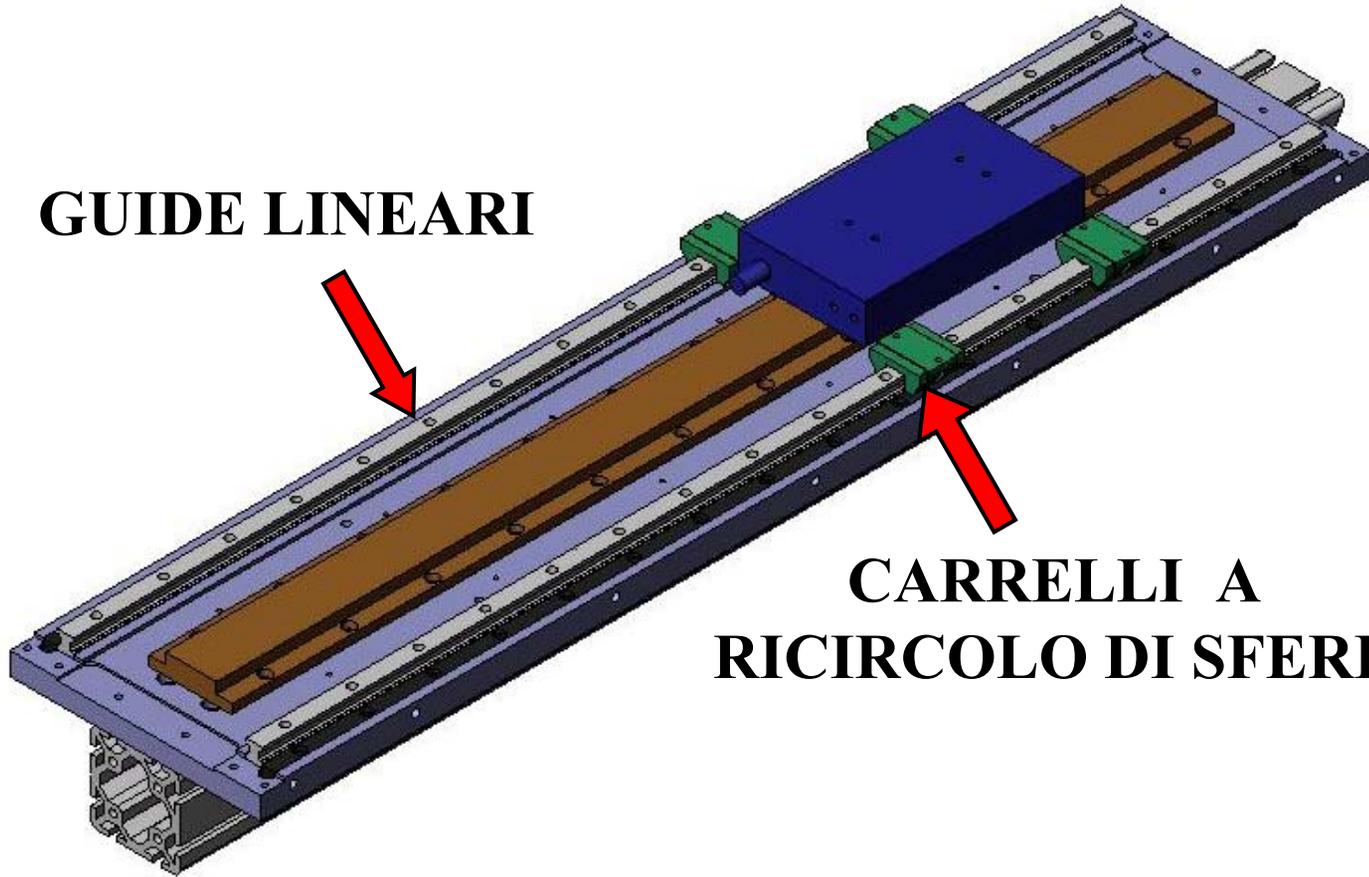


# Progettazione

## ASSE LINEARE



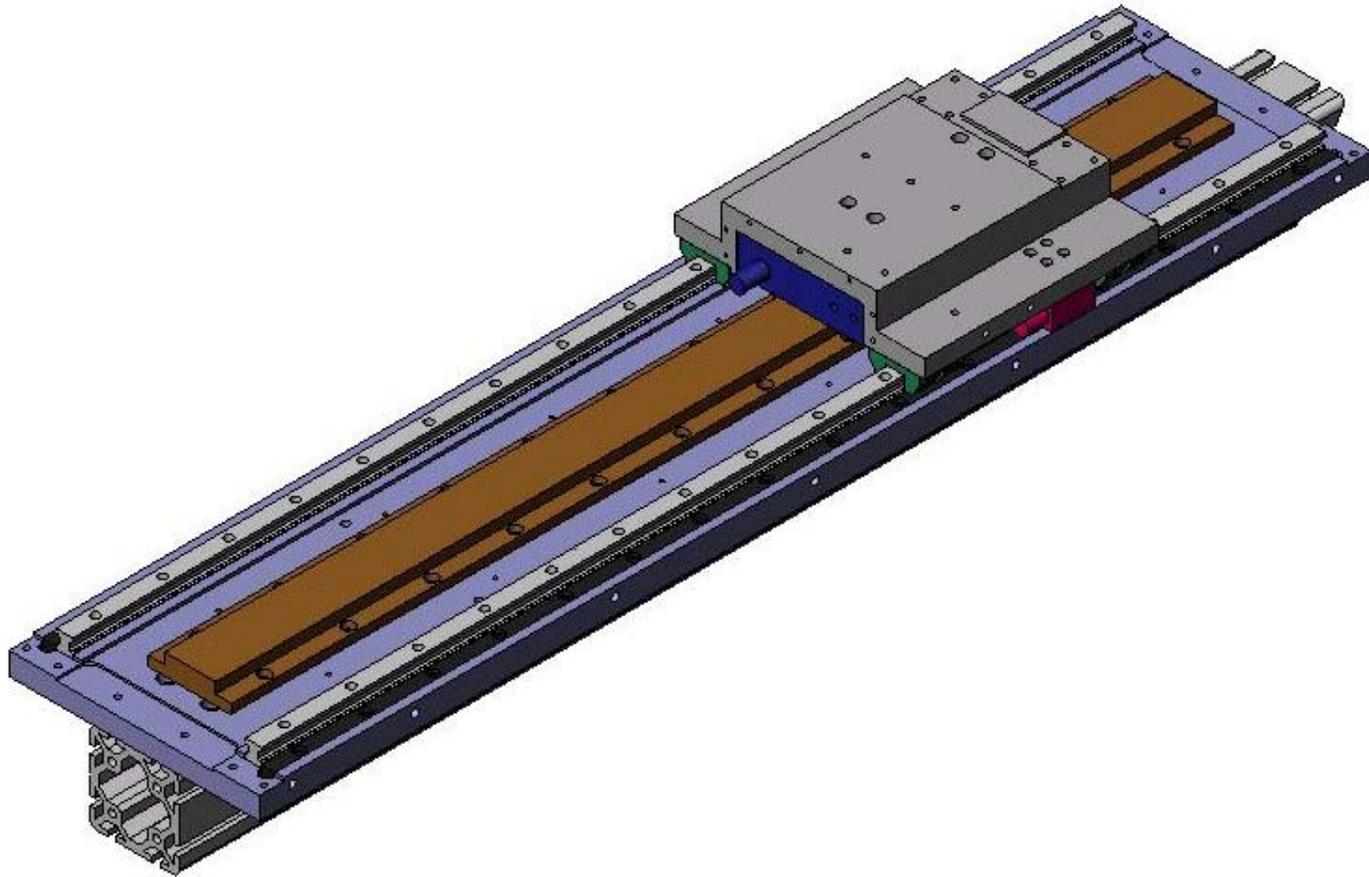
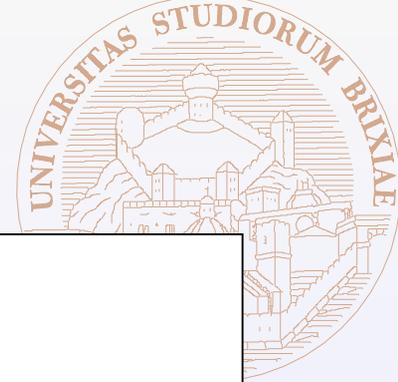
**GUIDE LINEARI**



**CARRELLI A  
RICIRCOLO DI SFERE**

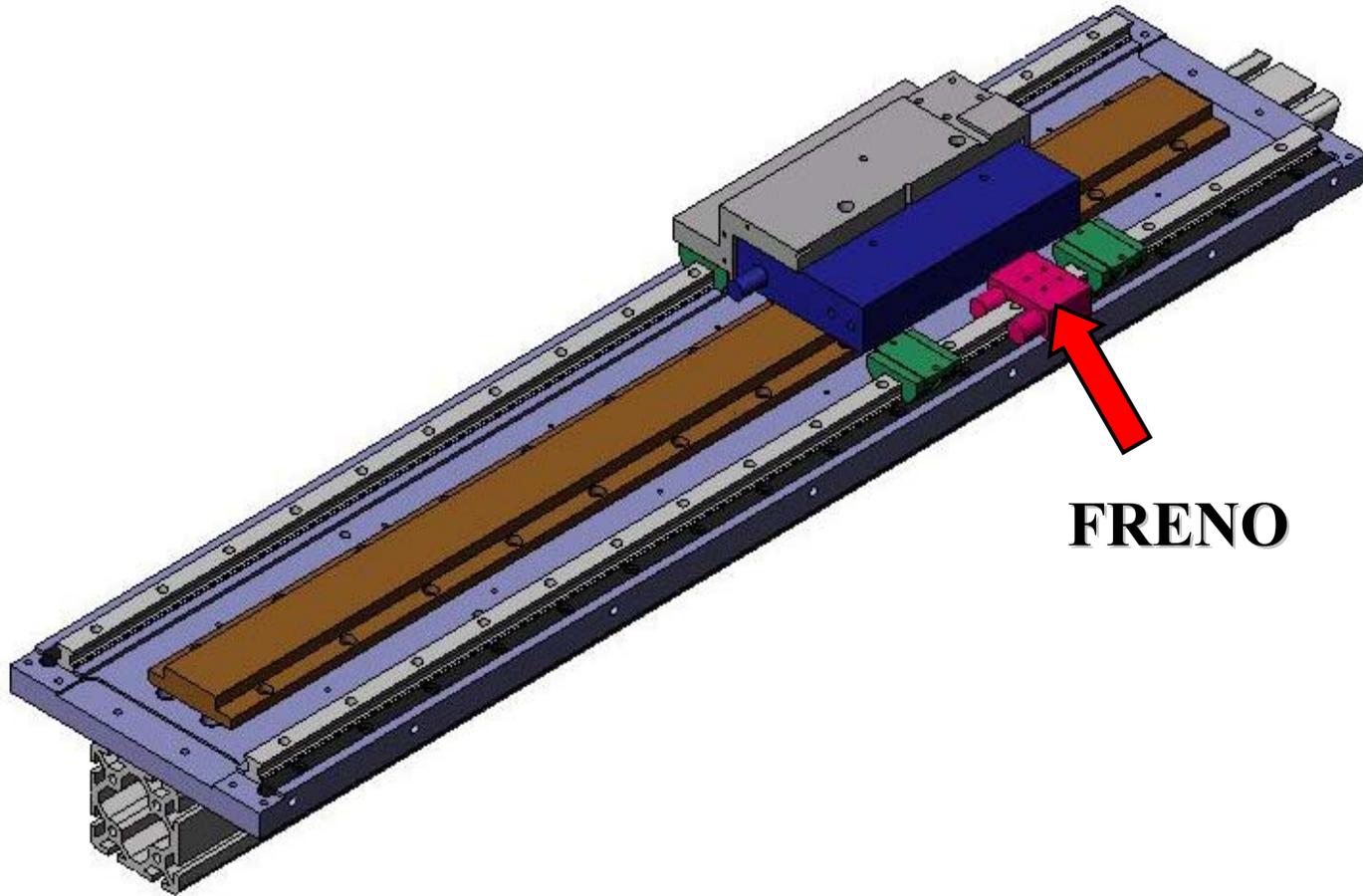
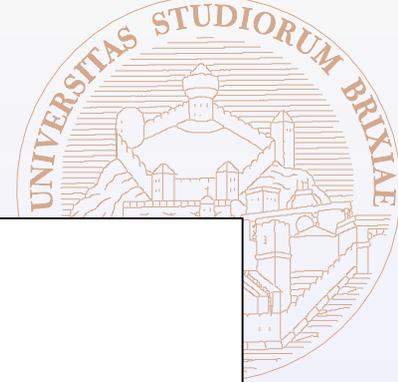
# Progettazione

## ASSE LINEARE



# Progettazione

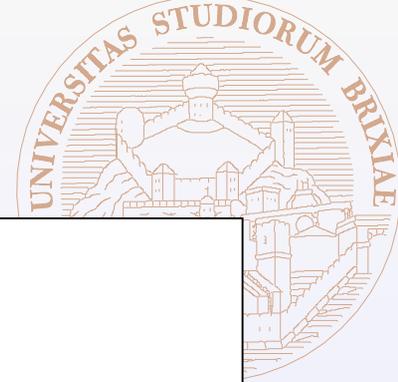
## ASSE LINEARE



**FRENO**

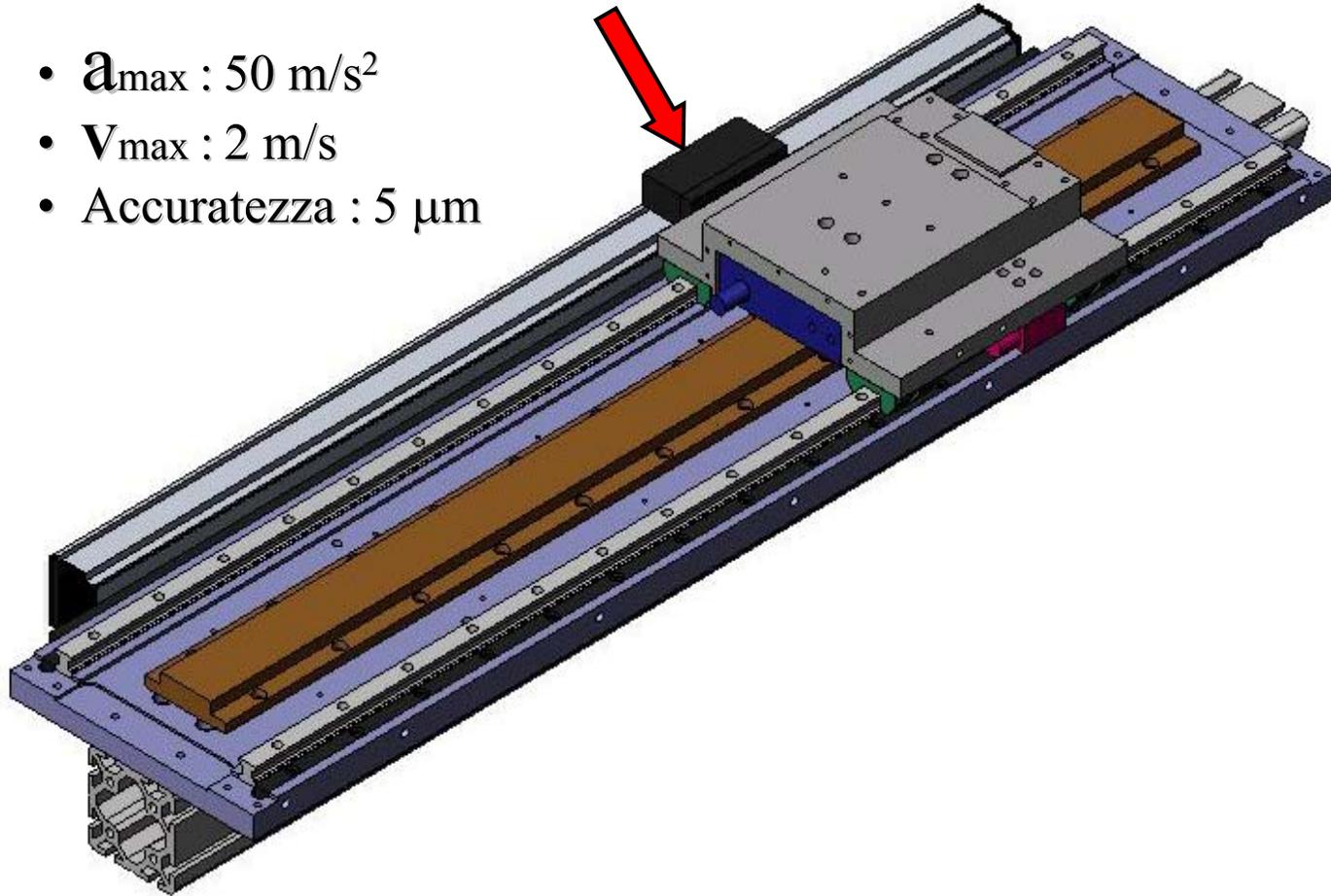
# Progettazione

## ASSE LINEARE



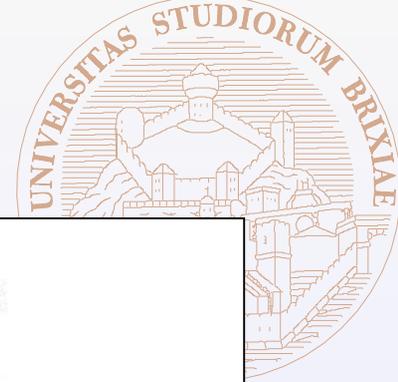
### RIGA OTTICA

- $a_{\max} : 50 \text{ m/s}^2$
- $V_{\max} : 2 \text{ m/s}$
- Accuratezza :  $5 \mu\text{m}$

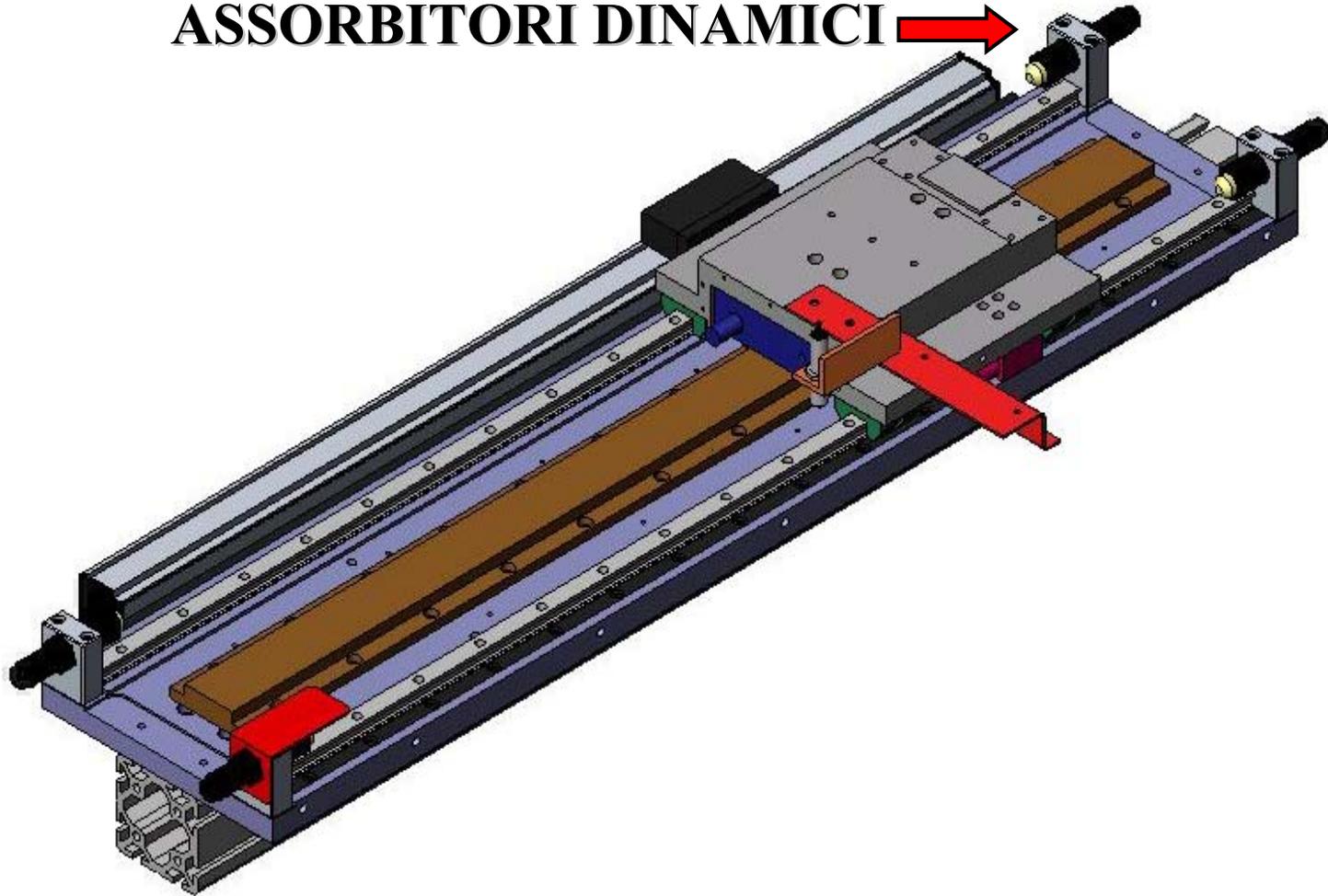


# Progettazione

## ASSE LINEARE

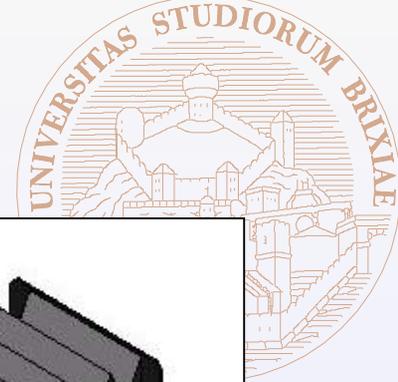


**ASSORBITORI DINAMICI** →

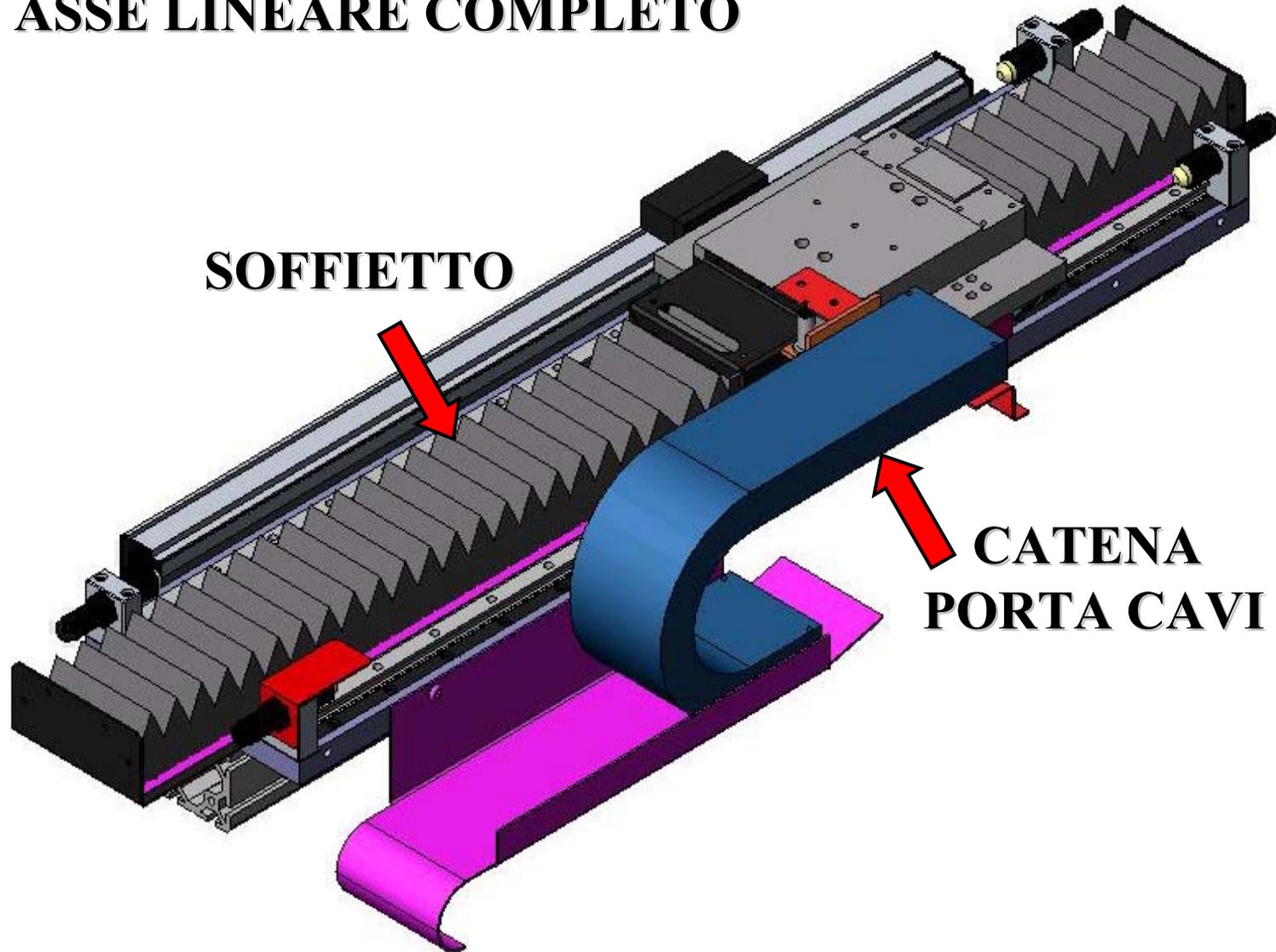


# Progettazione

## ASSE LINEARE



### ASSE LINEARE COMPLETO



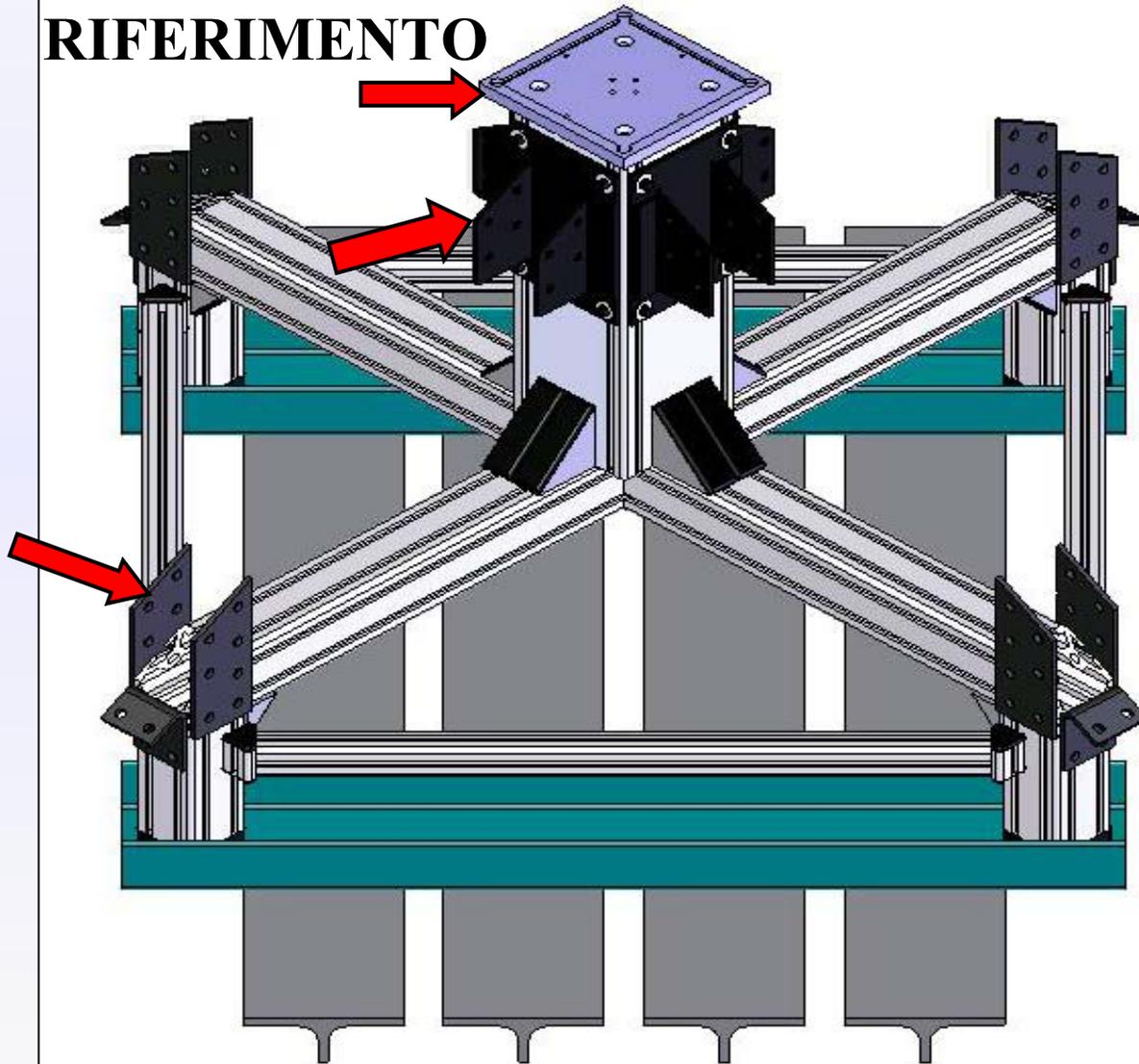
**SOFFIETTO**

**CATENA  
PORTA CAVI**

# Progettazione TELAIO

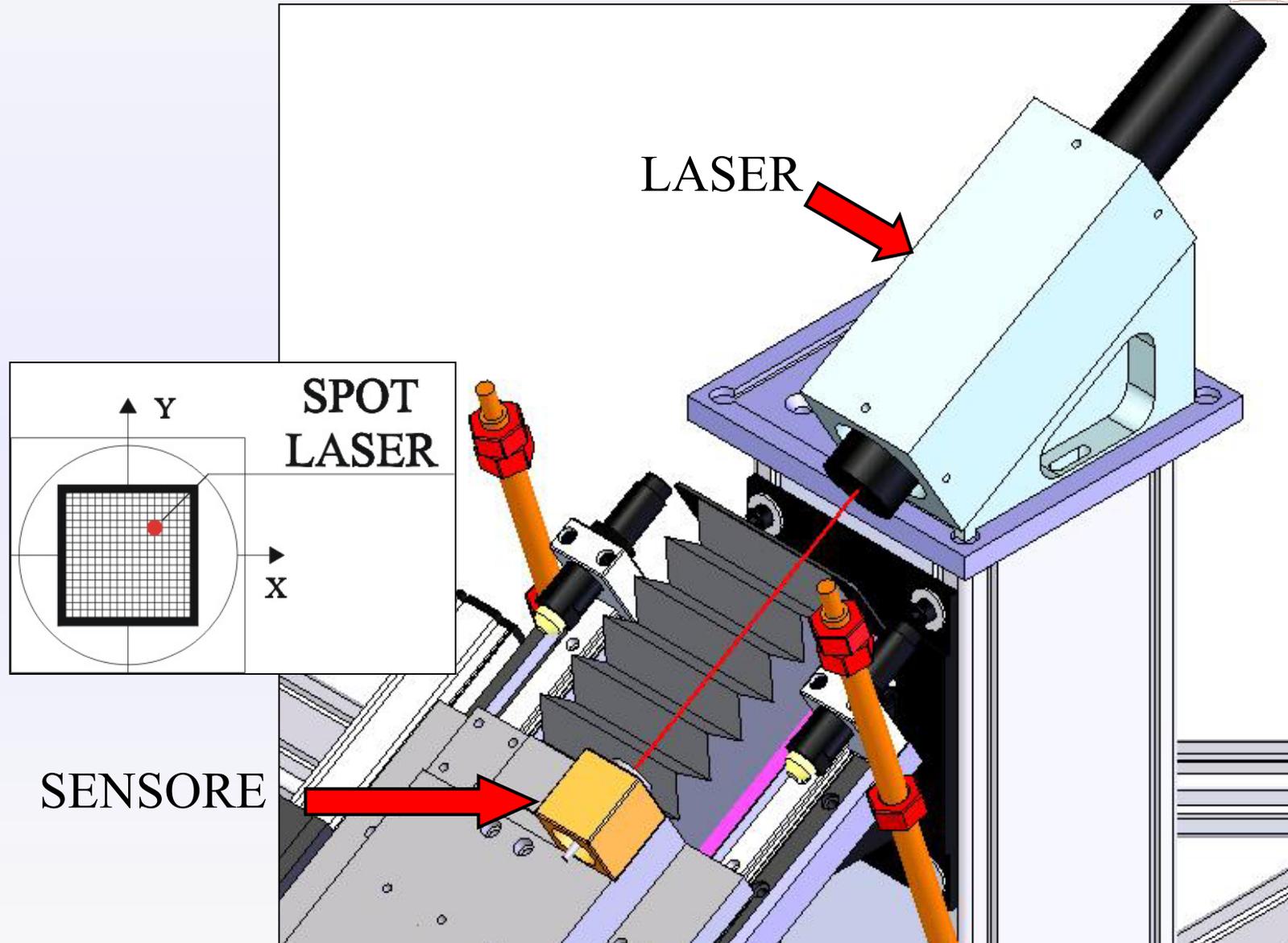


**PIASTRA DI  
RIFERIMENTO**

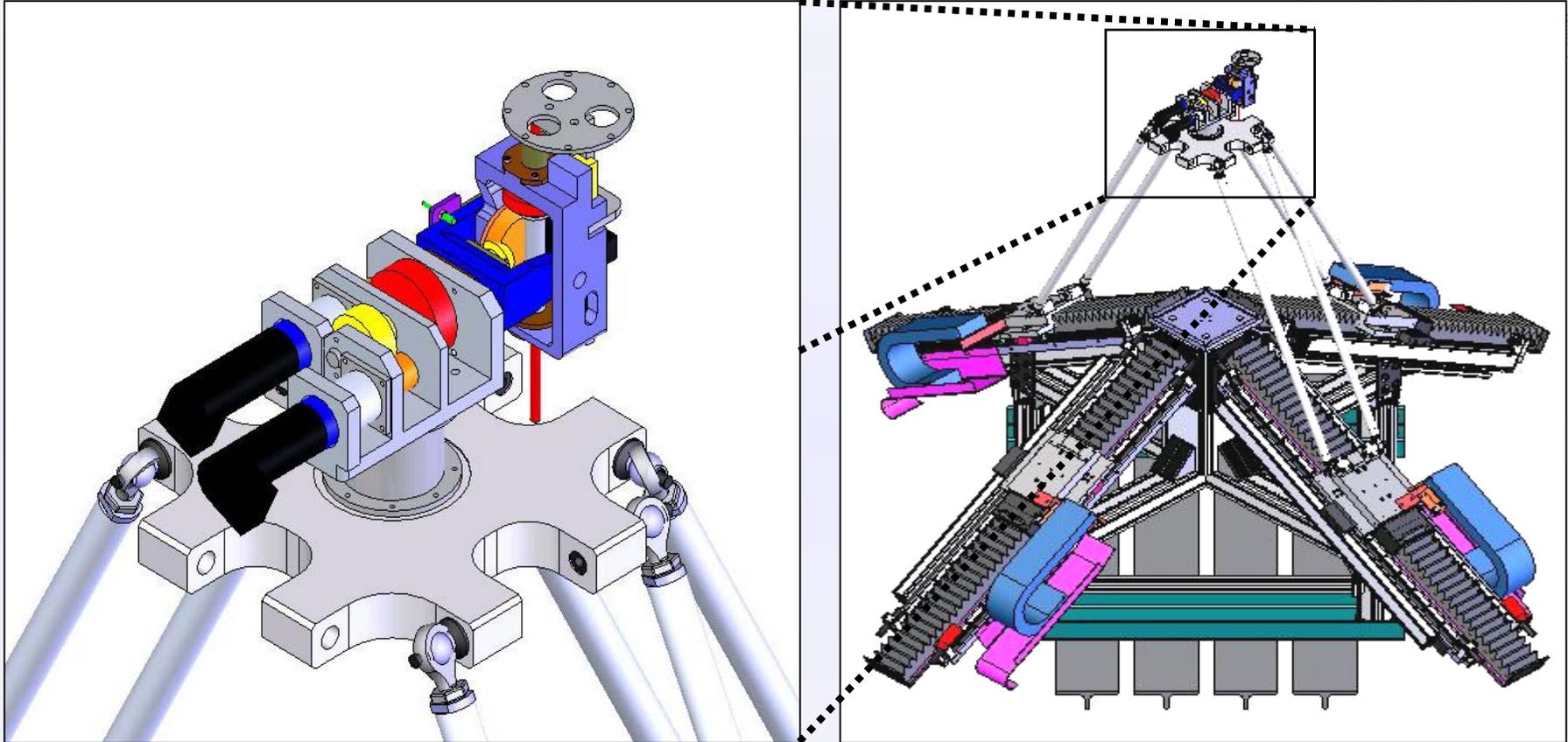


# Progettazione

## MONTAGGIO ASSI LINEARI

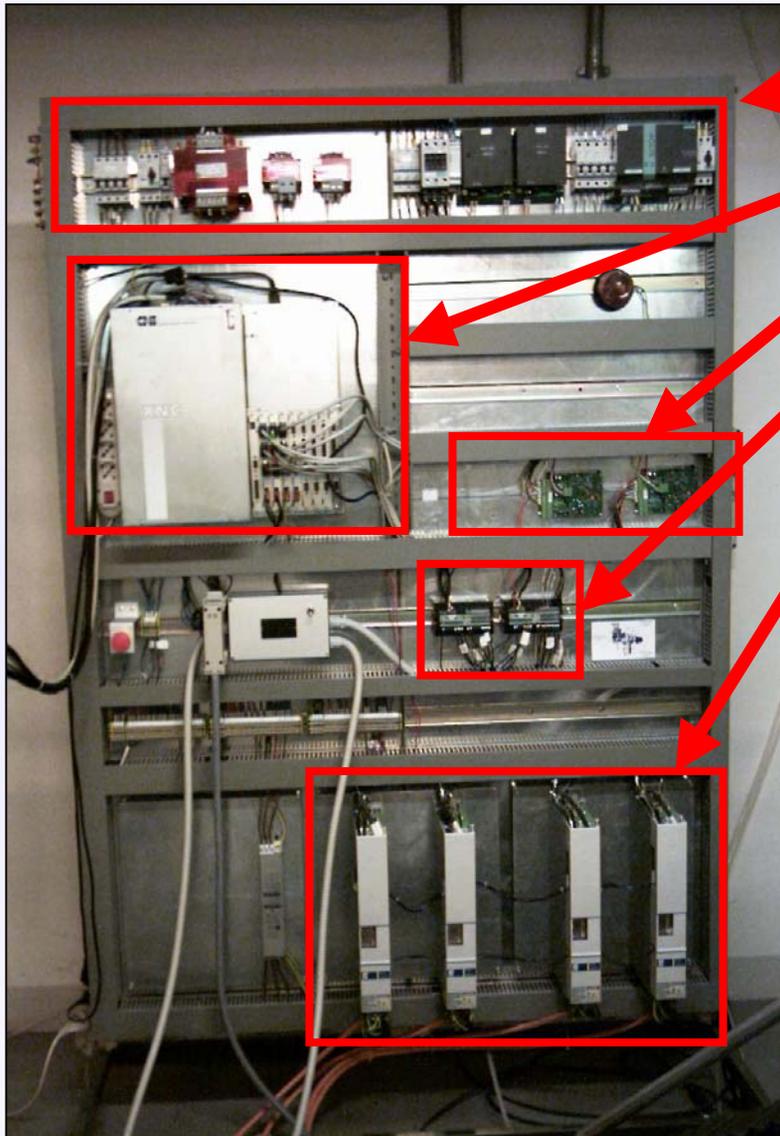


# Progettazione MONTAGGIO POLSO

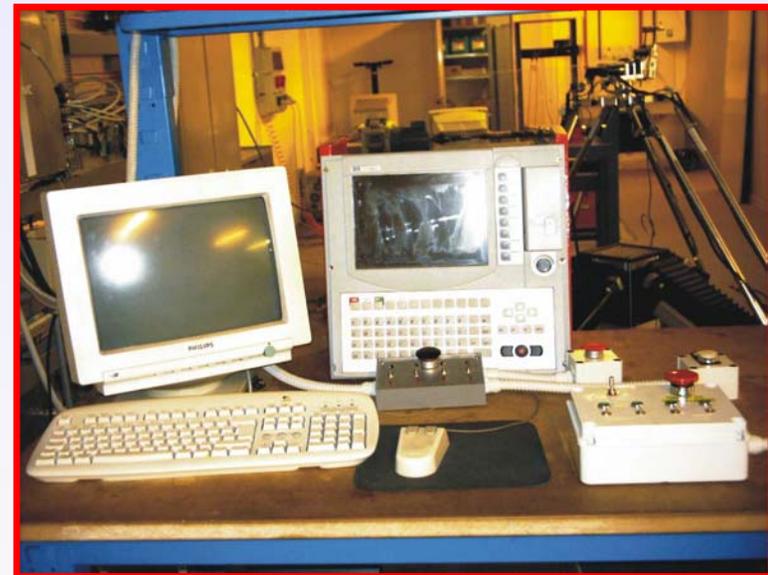


- ✓ ampie rotazioni
- ✓ gdl ridondanti
- ✓ movimenti coordinati

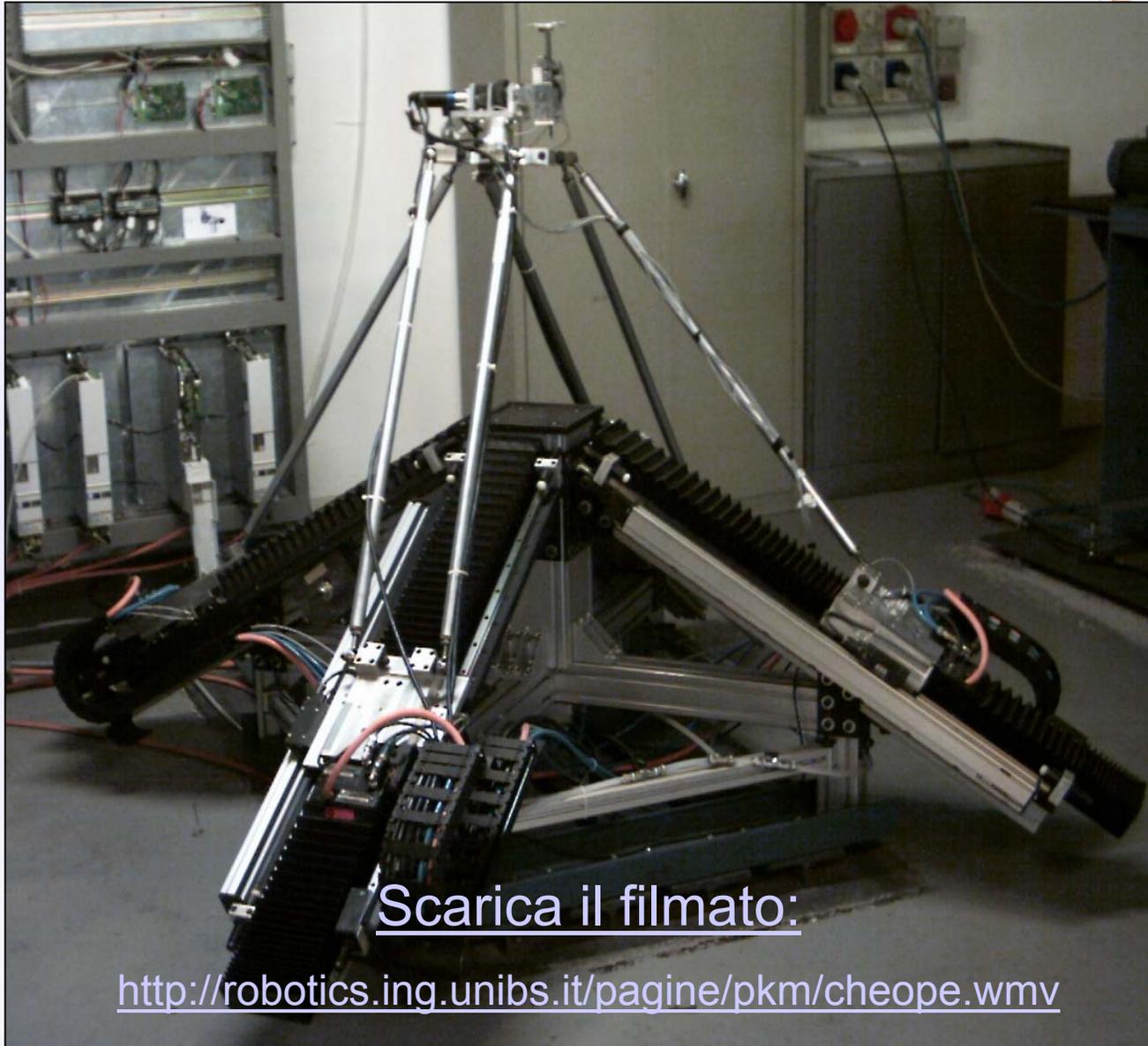
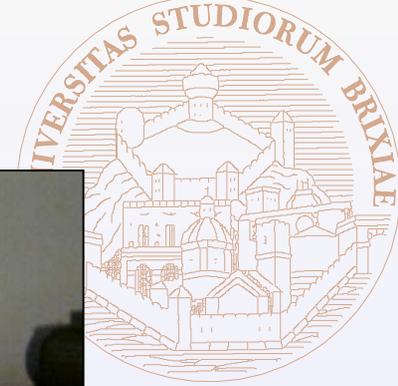
# Realizzazione IMPIANTO ELETTRICO



- ✓ **Impianto di potenza**
- ✓ **Controllore**
- ✓ **Convertitori motori polso**
- ✓ **I/O PLC gestione emergenze**
- ✓ **Convertitori motori lineari**
- ✓ **Interfaccia operatore**



# CHEOPE



Scarica il filmato:

<http://robotics.ing.unibs.it/pagine/pkm/cheope.wmv>